

Week 10 — Neural Networks & Deep Learning

Feedforward, RNN, and LSTM for Time Series

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From Linear to Neural

The Feedforward Neural Network

A single hidden layer:

$$\hat{y} = W_2 \cdot \sigma(W_1 \mathbf{x} + \mathbf{b}_1) + b_2$$

- σ : activation function (ReLU, sigmoid, tanh)
- **Universal approximation theorem**: one hidden layer can approximate any continuous function
- Trained by **backpropagation** + gradient descent

ReLU

$$\sigma(z) = \max(0, z)$$

Fast, sparse; default choice.

Sigmoid

$$\sigma(z) = \frac{1}{1+e^{-z}}$$

Output in $(0, 1)$; vanishing gradients.

Tanh

$$\sigma(z) = \tanh(z)$$

Output in $(-1, 1)$; zero-centred.

Recurrent Neural Networks

RNNs for Sequences

Standard feedforward networks treat inputs as *unordered*.

RNNs process sequences by maintaining a **hidden state**:

$$\mathbf{h}_t = \sigma(\mathbf{W}_h \mathbf{h}_{t-1} + \mathbf{W}_x \mathbf{x}_t + \mathbf{b})$$

- Natural fit for time series: respects temporal order
- **Problem:** vanishing/exploding gradients for long sequences

LSTM — Long Short-Term Memory

Solves the vanishing gradient problem with **gating mechanisms**:

- **Forget gate**: what to discard from cell state
- **Input gate**: what new information to store
- **Output gate**: what to output from cell state



Practical Considerations

When to Use Neural Networks?

Method	Strengths	Weaknesses
ARMA	Interpretable, theory	Linear
Exponential Smoothing	Trend + season	Univariate
VAR	Multivariate dynamics	Many parameters
Ridge/Lasso	Many predictors	Still linear
Random Forest	Nonlinear	No uncertainty
Neural Networks	Universal approx.	Data-hungry, opaque

Rule of thumb: start simple (ARMA, ETS). Add complexity only if justified by the data.

1. Time series **components and stationarity**
2. **Probability** and estimation
3. **ARMA**: the linear workhorse
4. **Forecasting**: estimation, selection, evaluation
5. **Exponential smoothing**: trend and season
6. **VAR**: multivariate dynamics
7. **State space**: unobserved components
8. **Dynamic factors**: large panels
9. **Machine learning**: regularisation, trees
10. **Neural networks**: nonlinear frontiers